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50 IS THE NEW 30 – LONG-RUN TRENDS OF SCHOOLING AND RETIREMENT EXPLAINED BY HUMAN AGING

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50 is the New 30 – Long-run Trends of Schooling and Retirement Explained by Human Aging

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March 2013

Abstract. Workers in the US and other developed countries retire no later than a century ago and spend a significantly longer part of their life in school, implying that they stay less years in the work force. The facts of longer schooling and simultaneously shorter working life are seemingly hard to square with the rationality of the standard economic life cycle model. In this paper we propose a novel theory, based on health and aging, that explains these long-run trends. Workers optimally respond to a longer stay in a healthy state of high productivity by obtaining more education and supplying less labor. Better health increases productivity and amplifies the return on education. The health accelerator allows workers to finance educational efforts with less forgone labor supply than in the previous state of shorter healthy life expectancy. When both life-span and healthy life expectancy increase, the health effect is dominating and the working life gets shorter if the preference for leisure is sufficiently strong or the return on education is sufficiently large. We calibrate an extended version of the model and show that it is capable to predict the historical trends of schooling and retirement.

Keywords: healthy life expectancy, longevity, education, retirement, labor supply, compression of morbidity.
JEL: E20, I25, J22, O10, O40.

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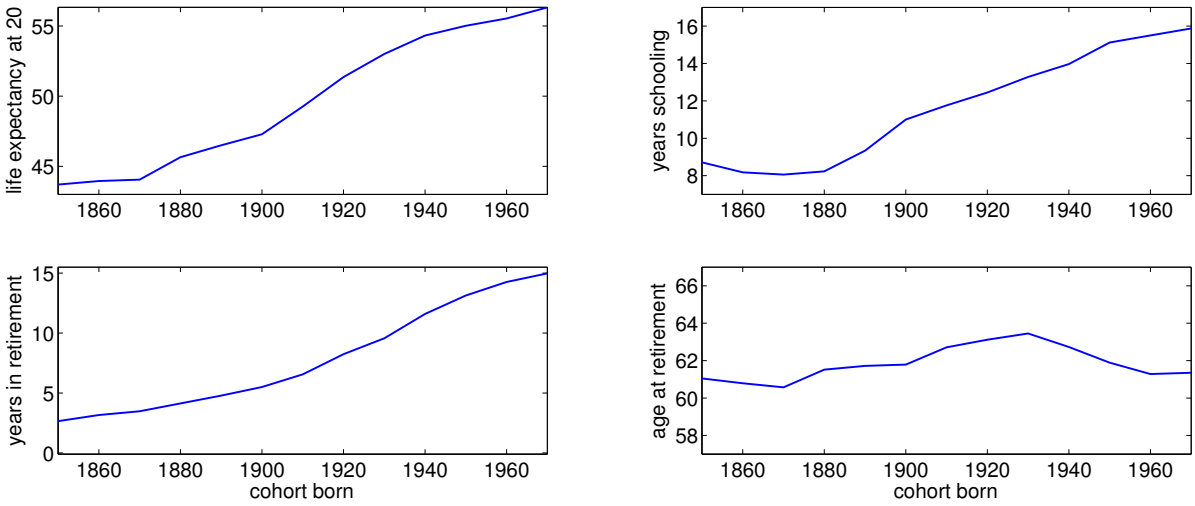
1. Introduction

In this paper we propose a novel life cycle theory of schooling, work, and retirement of aging individuals. The theory is useful to explain why younger generations spend more years in school but do not retire later, implying a shorter working life. This life cycle behavior is in particular intriguing because a popular explanation for a longer schooling period is based on increasing life expectancy, arguing that a longer expected lifespan allows to spend more time on education without reducing the working life i.e. without reducing the return on education (Cervelatti and Sunde, 2005). Indeed, if a simple life cycle model (Ben-Porath, 1967) is extended to allow for endogenous retirement, it predicts that increasing longevity induces more schooling and less or unchanged life time labor supply. Since life time labor supply is actually declining, it has been argued, that increasing life expectancy cannot explain the long-run trends of education, work, and retirement (Hazan, 2009).

Figure 1: Life expectancy at 20, Schooling, and Retirement: 1850 – 1970



Cohort data at 10 year intervals for US American males. Expected years in retirement is computed as life expectancy at 20 minus age at retirement. Life expectancy and age at retirement are from Lee (2001); life expectancy at 20 and years of schooling is from Hazan (2009).

Figure 1 shows the long-trends of life expectancy, education, age at retirement and expected years spent in retirement for cohorts of American men, born 1850-1970. For about a century, since 1870, education increased continuously, by about 8 years altogether. At the same time the age of retirement increased only slightly by about 2 years for cohorts born before 1940 and is predicted to decline about 2 years for the later born cohorts, implying hardly any trend over the whole observation period (Lee, 2001). During the same period of time the life expectancy at

age 20 of American men was rising from 43.7 years in 1850 to 57.7 years in 1990. These 14 more years were almost exclusively used to enjoy more leisure in retirement, as shown in the panel on the right hand side of Figure 1. Altogether this leaves us with the question why younger generations go longer to school when they do not want to work more.[1]

In this paper we propose an answer by extending the life cycle model used by Hazan (2009) and taking into account that human capital is a bivariate compound. It consists not only of education, as assumed in the conventional model, but also of a health component. Deteriorating functionality of the human body, i.e. aging, influences life cycle decisions potentially through two channels. Specifically, we take into account that after a period in best health, individual productivity declines with age. Declining productivity motivates the individual to retire and provides a mechanism that complements and amplifies the usual leisure-driven motive for retirement.

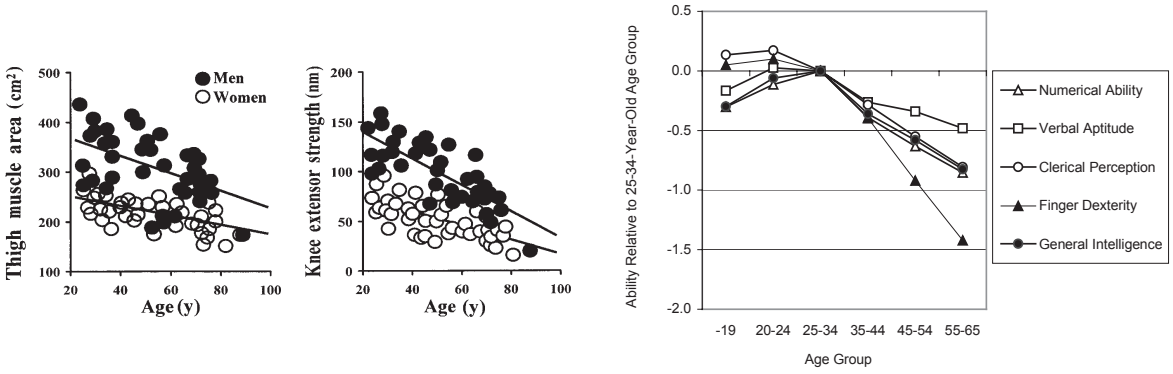
In order to explain the evolution of schooling and retirement behavior by trends of human aging and longevity we distinguish between life expectancy (lifespan) and healthy life expectancy. The WHO defines healthy life expectancy as the average number of years that a person can expect to live in "full health" (WHO, 2012). Over the last century healthy life expectancy increased along with life expectancy. Actually, members of later born cohorts can not only expect to live longer but also to live a relatively longer part of their life in a healthy state. Manton et al. (2006) estimate that for 65 year old US citizens the ratio between healthy (active) life expectancy and life expectancy rose from 73.9% in 1935 to 78.5% in 1999 and predict the ratio to increase further to 88% in the year 2080.

A longer stay in a healthy state increases labor productivity by reducing the force of aging through better maintenance and repair of the human body. Most of our cognitive skills and motor skills start deteriorating around the age of 30 or even earlier. The left and middle panel of Figure 2 (taken from Nair, 2005) show the decline of muscle mass and muscle strength with age. It is accompanied by a similar decline of oxygen uptake and an increase of muscle fatigue. Physiologically the phenomenon is explained by an increasing loss of redundancy in the human body and therewith deteriorating reliability, which eventually ends in death (see Arking, 2006,

[1] There is no contraction between Lee's (2001) observation of a (mild) increase in age of retirement and the observed decline in labor force participation of the elderly (Costa, 1998). The reason is that the labor force participation rate captures individuals who manage to survive until age 65; individuals who retired and died before the age of 65 do not count. During the period of observation improvements in health allowed more people to survive until the age of 65. This implies that the expected age of retirement increased while labor force participation declined.

on human aging; Gavrilov and Gavrilova, 1991, on reliability of the human body). Deteriorating muscle strength and reliability cause gross motor skills to decline with age.

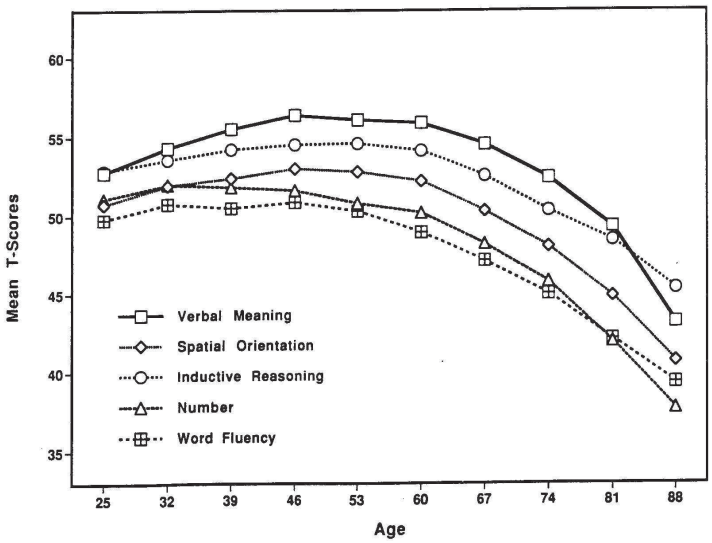
FIGURE 2: ASPECTS OF HUMAN AGING: DECLINING MUSCLE AND ABILITY



Source: left and middle panel: Nair (2005); right panel: Skirbekk (2004).

The panel on the right hand side of Figure 2, taken from Skirbekk (2004), shows that fine motor skills and and some cognitive abilities start declining around the age of 30 as well. But there are also important differences. In particular so called *crystallized abilities*, i.e. the abilities to use knowledge and experience, remain relatively stable until most of adulthood and start declining after the age of 60, or even later. As a result some measures of psychological competence, like verbal skills and inductive reasoning start declining "only" around age 50, as shown in Figure 3, taken from Schaie (1994).

FIGURE 3: ASPECTS OF HUMAN AGING: CRYSTALLIZED ABILITIES



Source: Schaie (1994).

Altogether this provides two mechanisms that work towards a long-run trend of increasing labor productivity through better health. The direct channel comes through improving health. The state of health of workers improved together with the long-run trend towards better nutrition, in particular during childhood, and its impact on productivity through alleviated body size and cognitive ability (Fogel, 1994, Case and Paxson, 2008, Case, 2010, Floud et al., 2011, Strauss and Thomas, 1998). The massive improvement in IQ in the US and other developed countries over the last century has been popularized as the Flynn effect (Flynn, 1984, 1987). Later born cohorts outperform earlier ones in intelligence tests, in particular in components involving reasoning ability (Schaie, 1994; Raven, 2000).

Perhaps even more important for the health of older workers is medical technological progress and the increased possibilities of maintenance and repair of the human body (e.g. Porter, 2001). Advances in medical technology allowed for a longer stay at high productivity on a learned occupation. For example, a century ago a chronic knee or hip injury would have severely reduced the productivity of a farmer or a mason. Today medical technological progress allows for a knee or hip replacement, keeping the worker – after operation and rehab – at full health and productivity. Medical technological progress improves healthy aging such that the (repaired) body starts declining later in life. We observe a compression of morbidity (Fries, 1980).

The second channel operates through skill-biased technological change. On average the work of today requires less gross motor skills (e.g. farm and construction work) and less fine motor skills (manufacturing) but more crystallized abilities (the service sector). The average worker was more likely to be a farmer or industrial worker hundred years ago and is more likely to be a salesperson or consultant today. Since crystallized abilities decline later in life, the average worker can expect to stay a longer period of her working life at high productivity. Recent research by Hamermesh (2013) suggests that this is even true for economists. Hamermesh observes a trend towards higher average age of authors publishing in the top five journals and explains this by a trend that made the profession less like pure mathematics (requiring mostly fluid abilities, which decline early in life) and more like a humanistic field (requiring mostly crystallized, which are more persistent).

Inspired by these observations we use subsequently a broader conceptualization of full health than the WHO (which does not consider aging-driven loss of cognitive abilities) and define as healthy life expectancy the age at which labor productivity starts declining. We then show that

an increasing healthy life expectancy, i.e. a longer expected stay in a healthy condition induces more schooling. More education and better health increase labor income per time increment (e.g. per year). Since the workers have a preference for leisure they respond to increasing income not only by consuming more but also by reducing their lifetime labor supply, i.e. by extending the period of schooling by more than their working life. If healthy life expectancy increases along with life expectancy it can then be that a longer life is observed along with a longer schooling period and a shorter working life. We show that this mechanism allows for an approximation of the historical trends of schooling and retirement by a reasonable numerical version of the model.

We acknowledge that the literature has suggested other, potentially complementing, mechanisms to explain the long-run trends of schooling and labor supply. Cervelatti and Sunde (2012) show that an increasing probability of survival during the working life may induce more schooling. Hansen and Loenstrup (2012) suggest a mechanism based on missing capital markets and accidental bequests. Restuccia and Vandenbroucke (2013) propose non-homothetic preferences (subsistence needs) and the demand of education for pleasure as the potential drivers of schooling and retirement behavior. There exists also a related literature discussing the interaction of health, life expectancy, and labor supply independently from schooling behavior (Heijdra and Romp 2009; Bloom et al, 2011; Kalemli-Ozcan and Weil, 2011; d'Albis et al., 2012; Kuhn et al., 2012, Dalgaard and Strulik, 2012) and a large (mostly empirical) literature investigating the association between health and education (for surveys see Grossman, 2006; Cutler and Lleras-Muney, 2006; Cutler et al., 2011).

The paper is organized as follows. The next section sets up the life cycle model with aging and explains the main mechanism of schooling and labor supply using the first order conditions. Section 3 presents the solution and discusses the comparative statics. Section 4 generalizes the basic model, calibrates it with US data, feeds in the historical time series of life expectancy at 20 for the US, and confronts the model predictions with the historical series presented in Figure 1. Section 5 concludes. Proofs of the Propositions and longer derivations of equations can be found in the Appendix.

2. The Model

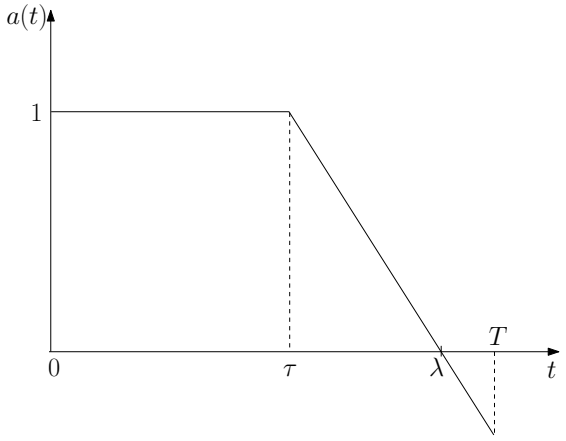
The starting point is the simple Ben-Porath (1967) model as re-introduced by Hazan (2009). Individuals expect to live for T years. Given this constraint they chose to attend school for s years (before work) and chose to retire from work after R years. In contrast to the earlier literature we take into account that human capital consists of two components, education and health. A person with s years education and health $a(t)$ supplies human capital $h(s,t)$ which equals individual productivity.

As in the standard model, attending school for s years produces education-specific human capital $e^{\theta(s)}$. Here, additionally, we take into account that health and productivity erode with age such that human capital of a person with s years of education and age t is given by $h(s,t) = e^{\theta(s)} \cdot a(t)$. Specifically, we assume that life consists of a period of best health of length τ, after which health deteriorates with age. In order to obtain an explicit solution of the life cycle problem we assume that health deteriorates linearly, i.e.

$$a(t) = \begin{cases} 1 & \text{for } t \leq \tau \\ 1 - \frac{t-\tau}{\lambda-\tau} & \text{for } t \geq \tau. \end{cases} \tag{1}$$

The parameter $1/(\lambda - \tau)$ captures the rate of aging and τ is conceptualized as healthy life expectancy. Figure 4 illustrates the implied health over the life cycle. After τ years, which are spend on schooling and work, productivity and health begin to deteriorate and at age λ productivity has declined to zero. The person dies at age T. The figure has been drawn such that the person continues to live for a while after reaching zero productivity, i.e. $T > \lambda$. This assumption is plausible but not necessary for our results. Note that the compression of morbidity, the effects of which we will investigate later on, is captured in the figure by rising τ. As a consequence of increasing τ the person spends a longer time of his or her life in a healthy condition after which health deteriorates faster until death. The earlier literature (e.g. Hazan, 2009) can be understood as a special case for which $\tau = \lambda = T$, that is the case in which the person stays in perfect health until death. Later on we discuss not only how individuals respond to an exogenous improvement in life expectancy T, as in the related literature, but also how they respond to an exogenous improvement of healthy life expectancy τ.

FIGURE 4: LIFE CYCLE WITH AGING



The standard Mincer (1974) equation contains two further terms, experience and "experience squared", which we ignore subsequently. We neglect the linear experience term to get an analytically tractable solution. We acknowledge that introducing experience would add more realism because it allows for an early period in work-life, in which productivity is going up, i.e. a hump-shaped productivity profile. We expect that our results are robust against the introduction of an early phase of increasing productivity because the mechanism that we investigate does not affect the early work period but the later period, in which health deteriorates and in which a retirement decision is made.[2]

The estimated Mincer equation usually obtains a negative coefficient for "experience squared", generating declining productivity at older ages. Since it is hard to believe that productivity is decreasing when there is "too much experience" we are convinced that this term is meant to measure the effect of increasing age on deteriorating health and productivity. The effect of deteriorating health is captured explicitly by (1) in our model.

Individuals maximize lifetime utility consisting of the discounted stream of instantaneous utility $u(c(t))$ experienced from consumption $c(t)$ at any age t plus utility experienced from leisure. We assume, as in the related literature, that labor is indivisible. Individuals decide whether to work or not. Since individual productivity is continuously decreasing during the second period of the working life, individuals start working after a period of schooling s and then retire at age R. Notice that rational individuals retire before or at the age λ, i.e. before or at the time when their productivity vanishes to zero, $R \leq \lambda$.

[2] In a related paper on retirement Rogerson and Wallenius (2007) show how a tent-shaped age-productivity profile can be transformed into a monotonously falling one without loss of information.

We also want to take into account that individuals experience less enjoyment from leisure when they are in a state of bad health. An analytically convenient way to do this is to assign a lower level of utility to a unit of leisure after age λ, i.e. after health (productivity) deteriorated to zero. Formally, individuals solve

$$\max_{s,R} V = \int_0^T \mathrm{e}^{-\rho t} u(c)\mathrm{d}t + f_1(\lambda - R) + f_2(T - \lambda) \tag{2}$$

in which ρ denotes the time preference rate and $f_1(x) > f_2(x)$. Without loss of generality we normalize units such that a unit of human capital gets a unit wage (net of labor supply costs). The lifetime budget constraint requires that discounted lifetime earnings equal discounted lifetime consumption, i.e.

$$\int_s^T e^{-rt} h(s,t)\mathrm{d}t = \int_0^T e^{-rt} c(t)\mathrm{d}t. \tag{3}$$

To simplify the problem (1)-(3) we follow Hazan (2009) and assume that $r = \rho$ such that individuals prefer a smooth consumption profile over life. We furthermore assume a log form for utility experienced from consumption $u(c) = \log(c)$, and an isoelastic form for utility experienced from healthy leisure time $f_1 = \omega(\lambda - R)^{1-\eta}/(1-\eta)$. The term $1/\eta$ is the intertemporal elasticity of substitution for leisure.[3] For the analytical part of the paper we furthermore normalize the interest rate to zero and assume a constant return to schooling, $\theta(s) = \theta \cdot s$.

While these assumptions somewhat reduce the generality of our results, they are also quite powerful in that they allow for a neat explicit solution of the life-cycle problem with aging. This in turn, allows us to formally prove our results. We are thus convinced that the end justifies the means, in particular since the related literature on aging, schooling, and labor supply is usually confined to numerical simulations. In Section 4 we present a generalized version of the model with positive interest rates and decreasing returns to schooling. This provides more realism and a better approximation of the historical data but leaves the main mechanisms unaffected.[4]

With the assumptions made problem (1)-(3) can be restated as

$$\max_{s\geq 0, R\geq \tau} T\log\left\{e^{\theta s}(\tau - s) + e^{\theta s}\frac{(2\lambda - R - \tau)}{2(\lambda - \tau)}(R - \tau)\right\} + \omega\frac{(\lambda - R)^{1-\eta}}{1-\eta} + \gamma, \quad \omega \geq 0, \eta \geq 0. \tag{4}$$

[3] If there were a labor supply decision at the intensive margin and ℓ were hours worked then $(1-\ell)/(\ell\eta)$ would provide the Frisch elasticity of labor supply.

[4] The main consequence of the a zero interest rate is that individuals demand too much education since costs of education are too low. The main consequence of a constant return to education is that individuals follow a "too steep" education trajectory when their healthy life expectancy increases. Positive interest rates and decreasing returns to education remove these shortcomings in quantitative performance of the model.

The first term in curly parenthesis is the income earned during the first period of the working life, which is of length $(\tau - s)$. The second term is the income earned during the second period of the working life, which is of length $(R - \tau)$. The parameter γ summarizes several parameters that are given for the individual and do not affect the first order conditions, $\gamma \equiv f_2(T - \lambda) - \log T$.

The first order condition for optimal schooling is given by (5).

$$e^{\theta s} = (\tau - s) \cdot \theta e^{\theta s} + \frac{(2\lambda - R - \tau)(R - \tau)}{2(\lambda - \tau)} \cdot \theta e^{\theta s} \equiv g(\tau, \lambda, s, R) \cdot \theta e^{\theta s}. \tag{5}$$

The left hand side of (5) is the opportunity cost of one extra time unit of education. The right hand side provides the income gain of one extra time unit of education which accrues in the first and second period of the working life. As found by the earlier literature, the education decision, does not *directly* depend on life-span T. But it depends on the length of the healthy working life τ. A longer healthy life increases human capital per unit of education and thus increases the gain from an extra time unit spent on education. To see this formally, first notice that $g(\cdot)$ in (5) provides the income gain per unit of human capital elicited by an extra unit of education; then take the derivative with respect to τ.

$$\frac{\partial g}{\partial \tau} = 1 - \frac{2\lambda^2 + R^2 + \tau^2 - 2\lambda(R + \tau)}{2(\lambda - \tau)^2} > 0 \quad \text{since } \lambda > R > \tau.$$

Likewise observe that the gain from schooling is increasing in the age of retirement $\partial g / \partial R = (\lambda - R)/(\lambda - \tau) > 0$. This result is immediately intuitive and probably the most well-known mechanism of the Ben-Porath model.

The first order condition for the optimal retirement age is given by (6),

$$\omega(\lambda - R)^{-\eta} = \frac{2(\lambda - R)}{2\lambda(R - s) - \tau(\tau - 2s) - R^2} \cdot T \equiv \tilde{g}(\tau, \lambda, s, R) \cdot T. \tag{6}$$

The left hand side of (6) is the utility gain from an extra unit of time (say, a year) spent in retirement. The right hand side is the marginal cost of retiring a time unit earlier. More schooling increases the marginal cost of retiring. Formally, this can be seen by inspecting the opportunity cost of retirement per year and unit of human capital $\tilde{g}(\cdot)$ and taking the derivative with respect to s, that is $\partial \tilde{g} / \partial s = 4(\lambda - R)(\lambda - \tau)/N^2$ with $N = 2\lambda(R - s) - \tau(\tau - 2s) - R^2$, and concluding that it is positive. Intuitively, a longer schooling period reduces life time income per unit of human capital and a lower level of income and thus consumption increases the marginal utility of consumption, implying a higher marginal opportunity cost of retiring early.

A longer period in good health τ decreases the marginal cost of retiring early, $\partial\tilde{g}/\partial\tau = -4(\lambda-R)(\tau-s)/N^2 < 0$. A longer healthy working life increases income and therewith decreases marginal utility from consumption, implying a lower marginal cost of retiring early. By the same token, the marginal cost of retirement is decreasing in the age of retirement, $\partial\tilde{g}/\partial R < 0$. A longer working life increases income and consumption and reduces the marginal utility from consumption. Finally, the marginal utility from retiring early, the left hand side of (6), is increasing in R. These partial responses are the main ingredients to understand retirement and schooling behavior of aging individuals.

To begin with, consider an increase of healthy life expectancy τ. As explained above the direct response is more time spent at school and a later retirement age. But the longer time spent at school raises the productivity of human capital and thus income, implying a lower marginal utility from consumption and increasing demand for leisure. Thus, taken for itself, the indirect effect works in favor of an *earlier* retirement age. Since the income effect counteracts the direct effect of schooling on retirement, the change in desired retirement age is comparatively mild and the dominating effect on lifetime labor supply is the longer stay at school. This means that labor supply decreases as a response to higher healthy life expectancy.

Next consider an increase of life expectancy T. The first order condition for schooling is independent from T. Thus, "in the first round" a longer life affects only the retirement decision. It increases the value of consumption and income on the extensive margin, which leads to more labor supply and a later age of retirement. Formally, the equation is balanced because $\tilde{g}(\cdot)$ is decreasing in R and because the marginal utility of leisure is increasing in R. As explained above, later retirement, induces more schooling. As shown below, it can then be that lifetime labor supply decreases because schooling reacts more heavily than retirement. Ceteris paribus this is more likely if there is little weight ω on leisure in utility and if the return on education θ is high.

3. The Solution

We focus on the interior solution for education. Inspection of (5) shows that s would get negative if the return on education θ were too low or if the length of life T were too short. In these cases a non-negativity constraint on s applies and education assumes a corner solution. Investigating a state at which no education is optimal is interesting from the viewpoint of

macroeconomic history. But here we are interested in the interaction of education and lifetime labor supply and assume henceforth that parameter values are such that the interior solution applies. After some algebra we obtain from (5) and (6) an explicit solution for the optimal years of schooling s, the age at retirement R, and life time labor supply L.

$$R = \lambda - \left(\frac{(\lambda - \tau)\omega}{\theta T} \right)^{\frac{1}{1+\eta}} \tag{7}$$

$$s = \frac{\lambda + \tau}{2} - \frac{1}{\theta} - \frac{1}{2(\lambda - \tau)} \left(\frac{(\lambda - \tau)\omega}{\theta T} \right)^{\frac{2}{1+\eta}} \tag{8}$$

$$L = \frac{1}{\theta} + \frac{1}{2(\lambda - \tau)} \left[\mu - \tau - \left(\frac{(\lambda - \tau)\omega}{\theta T} \right)^{\frac{1}{1+\eta}} \right]^2 . \tag{9}$$

We first investigate the general case of $\eta > 0$ and later on the special case $\eta = 0$. For the general case the following propositions are proved in the Appendix.

Proposition 1 (Education). *The time spent in school increases with healthy life expectancy τ and with longevity T. Furthermore, it increases with the return to schooling θ.*

Proposition 2 (Retirement Age). *The retirement age R increases with healthy life expectancy τ, with longevity T and with the return to schooling θ. Furthermore, it decreases with the weight of leisure in utility ω.*

Proposition 3 (Labor Supply). *Lifetime labor supply $L = R - s$ decreases with healthy life expectancy τ and increases with longevity T.*

Proposition 4. *An equiproportionate increase of life expectancy and healthy life expectancy leads to more schooling and less lifetime labor supply iff*

$$\theta > \frac{(\lambda - \tau)\omega}{T} \left[\frac{2(\lambda - \tau) + T(1 - \eta)}{T(1 + \eta)(\lambda - \tau)} \right]^{1+\eta} .$$

If we just focus on lifespan T there is nothing new here. The propositions confirm the result from the available literature: With rising lifespan the individual wants to educate more and work longer. Since life time labor supply actually declined one may conclude from this result that increasing life-expectancy cannot explain the historical schooling trends (Hazan, 2009).

The picture changes once we focus on healthy life-expectancy τ. With healthy life-expectancy the individual wants to get more education and to reduce lifetime labor supply. A longer

healthy life increases productivity and the pay off of an extra year of education and thus induces more schooling. Higher income allows more consumption, the marginal utility from consumption declines and leisure becomes relatively more precious. Consequently the individual reduces labor supply. We explained the mechanism in detail when we discussed the first order conditions.

Actually, as argued in the Introduction, life expectancy and healthy life expectancy increase simultaneously. Proposition 4 shows that it can then happen that the effect of healthy life expectancy is dominating and increasing life expectancy is observed along with more schooling and less lifetime labor supply. In order to make the underlying mechanics better visible we consider the special case $\eta = 0$, i.e. linear utility from leisure. The solution of the life cycle assumes then a particularly simple solution:

$$R = \lambda - \frac{(\lambda - \tau)\omega}{\theta T} \tag{10}$$

$$s = \frac{\lambda + \tau}{2} - \frac{\omega^2(\lambda - \tau)}{2\theta^2 T^2} - \frac{1}{\theta} \tag{11}$$

$$L = 1 + (\lambda - \tau)\frac{(\theta T - \omega)^2}{2\theta^2 T^2}. \tag{12}$$

PROPOSITION 5 (Education). *The time spent in school increases with healthy life expectancy τ, longevity T, and the return to schooling θ. It decreases with the weight of leisure in utiltiy ω.*

PROPOSITION 6 (Retirement). *The retirement age R increases with healthy life expectancy τ, longevity T, and the return to schooling θ. It decreases with the weight of leisure ω.*

PROPOSITION 7 (Labor Supply). *Lifetime labor supply $L = R - s$ decreases with healthy life expectancy τ. It decreases with total life span T, and increases in the weight of leisure ω iff $\omega > \theta T$.*

PROPOSITION 8. *An equiproportionate increase of life expectancy and healthy life expectancy leads to more schooling and less lifetime labor supply iff (i) $\omega > \theta T$ or iff (ii)*

$$\theta > \frac{\omega\left[2(\lambda - \tau) + T\right]}{T^2}.$$

Proposition 7 confirms the initial conjecture that it is possible that labor supply decreases as a response to increasing lifespan. For that the intertemporal elasticity of substitution for leisure must be sufficiently high (actually, infinite) and the weight of leisure in utility must be sufficiently large.

Proposition 8 shows conditions under which an equiproportionate increase of life expectancy and healthy life expectancy reduces lifetime labor supply. Condition (i) is perhaps less interesting. It is based on a negative response of labor supply to increasing lifespan, an artefact of the assumption $\eta = 0$. An increasing lifespan, ceteris paribus, reduces consumption per time unit and thus increases marginal utility from consumption, thereby inducing more schooling and later retirement. Since the marginal utility from leisure is non-decreasing in this special case, the effect on retirement is negative if the weight of leisure in utility ω is large enough.

Condition (ii) is more interesting and corresponds with the condition of Proposition 4. It requires a sufficiently large return to schooling. The condition is comparatively more easily fulfilled if the weight of leisure in utility low, if life is long, and if there is compression of morbidity (τ is close to λ). Under these conditions the response of more schooling to increasing healthy life-expectancy is dominating the retirement effect. The mechanism is most obvious for $\omega \to 0$. In that case retirement does not respond at all and schooling increases because of increasing healthy life expectancy. Notice that a high return on schooling, a long life, and a compression of morbidity are conditions that characterize life in modern economies. It may thus be that increasing (healthy) life expectancy is observed along with more labor supply in less developed economies but along with less labor supply in developed economies.

Extensions and Calibration

This section has a twofold purpose. It generalizes the model and confronts the predictions made by a calibrated version with the historical time series shown in the Introduction. As a first numerical experiment we give up the assumption of zero interest rates. Assuming $r = \rho > 0$ and keeping all other simplifying assumptions, the first order conditions for problem (1)–(3) read

$$\frac{\partial U}{\partial s} = \frac{e^{-rT}(e^{rT}-1)}{r}\left(\theta - \frac{e^{r(R+\tau)}r^2(\lambda-\tau)}{e^{r(R+s)} + e^{r(s+\tau)}(-1+r(\lambda-R)) + e^{r(R+\tau)}r(\tau-\lambda)}\right) = 0$$

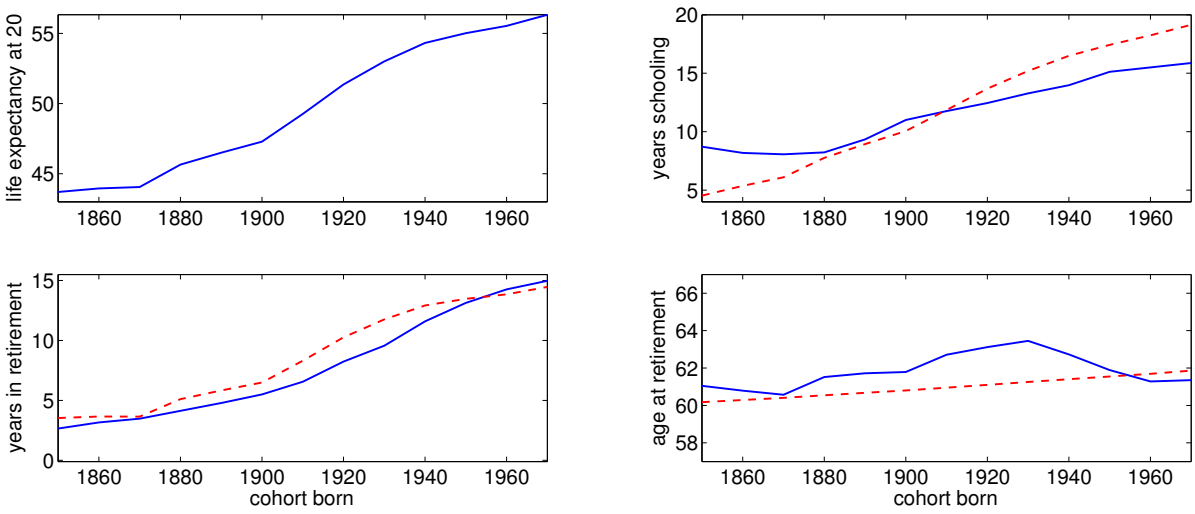
$$\frac{\partial U}{\partial R} = \frac{e^{-rT}(\lambda-R)^{-\eta}}{e^{r(R+s)} + e^{r(s+\tau)}\left(-1+r(\lambda-R)\right) + e^{r(R+\tau)}r(\tau-\lambda)} \cdot \Gamma = 0$$

with

$$\Gamma := e^{r(s+\tau)}r(\lambda-R)^{1+\eta} - e^{r(R+s+T)}\omega - e^{r(R+T+\tau)}r(\tau-\lambda)\omega + e^{r(s+T+\tau)}\left(\omega + r(R-\lambda)\left((\lambda-R)^{\eta}+\omega\right)\right).$$

From here we have to proceed numerically. Following Mehra and Prescott (1985) we set $r = 0.07$, representing the average real return on the stock market for (most of) the last century. We set $\eta = 8$, a value that corresponds to a labor supply elasticity of 0.25, as recently estimated by Chetty et al. (2011) for labor supply at the extensive margin. We feed into the model the historical time series for life expectancy at 20 from Hazan (2009). We capture the stylized fact from the Introduction that healthy life expectancy improves with life expectancy in a mildly asymmetric way be assuming that $\tau(k) = T(k) - 15 + k$, in which k is the index number of the birth year of a cohort starting 1840 ($k = 1$) and ending 1970 ($k = 13$). This means that healthy life expectancy (at birth) improves from 29.7 to 54.3 when life expectancy expectancy (at 20) improves from 43.7 to 56.3. For the end of the observation period it is thus predicted that labor income starts declining at roughly age 55, an outcome that squares well with the actual behavior of wages in the US (French, 2005). We also assume that λ improves mildly from 55.8 to 57 during the observation period. Overall this means a strong compression of morbidity; $(\lambda - \tau)$ improves from 26 to 2.6.

FIGURE 5: DATA AND MODEL PREDICTION: 1840-1970



Solid lines: data from Figure 1. Dashed lines: model prediction.

Finally we search for values of θ and ω that produce a reasonable prediction of the historical trends of schooling and retirement. Figure 5 shows results for $\omega = 0.1$ and $\theta = 0.076$, represented by red (dashed) lines. Solid (blue) lines re-iterate the historical US time series from the Introduction. Results are relatively insensitive with respect to the choice of ω. A tenfold increase or decrease of ω shifts the age-at-retirement series by about a year. Results are much

more sensitive to the choice of the return to schooling θ. It is thus reassuring that our numerical estimate of θ is not outlandish in comparison with the econometric estimates. A value of 0.076 lies within the confidence bands of most of the OLS and IV estimates of the studies surveyed by Card (1999).

The upper left panel in Figure 5 shows the evolution of life expectancy that we feed into the model. The upper right panel shows the actual and predicted evolution of schooling. The model gets the direction of the trend right but predicts a too steep increase of schooling. The lower right panel shows the evolution of retirement. The model cannot capture the mildly hump shaped trajectory of retirement but gets the long-run trend right by predicting an almost invariant age of retirement. Together with the predicted trajectory for schooling this means that the model gets the evolution of years in retirement about right, as shown in the lower left panel.

The fact that the model predicts a too steep increase of schooling originates presumably from the assumption of constant returns to schooling. Decreasing returns would produce a declining incentive to educate when schooling is already high and could thus yield a better fit of the historical time series. In order to exploit this idea we assume, following Bils and Klenow (2000) that $\theta(s) = \theta^{1-\psi}/(1-\psi)$. The first order conditions for optimal schooling and retirement are then given by

$$\frac{\partial U}{\partial s} = \frac{e^{-rT}(e^{rT}-1)}{r}\left(\theta s^{-\psi} - \frac{e^{r(R+2\tau)}r^2(\tau-\lambda)}{e^{r(R+s+\tau)} + e^{r(s+2\tau)}(-1+r(\lambda-R)) + e^{r(R+2\tau)}r(\tau-\lambda)}\right) = 0,$$

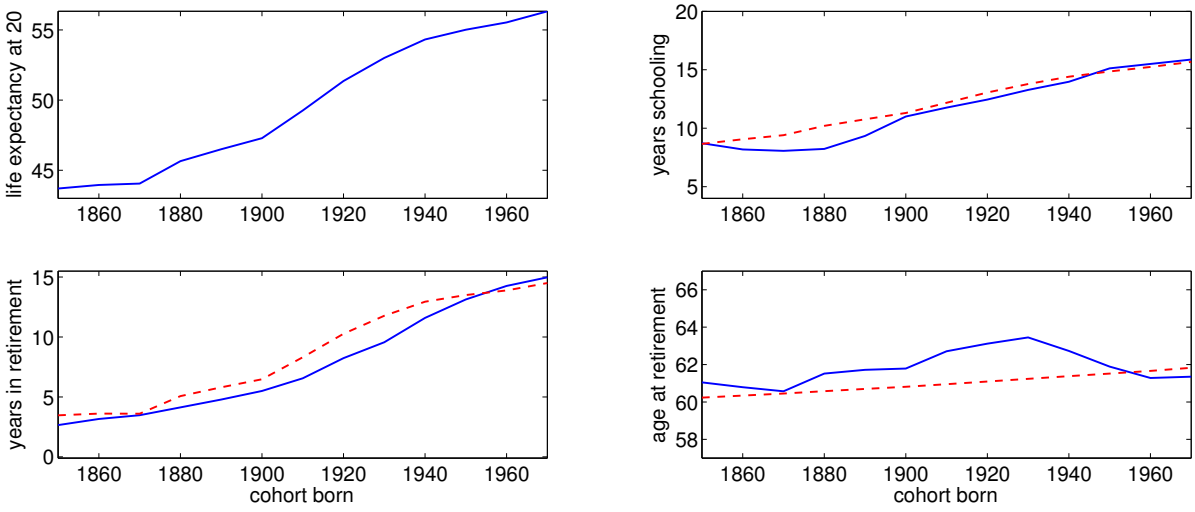
$$\frac{\partial U}{\partial R} = \frac{e^{-rT}(\lambda-R)^{-\eta}}{e^{r(R+s+\tau)} + e^{r(s+2\tau)}\left(-1+r(\lambda-R)\right) + e^{r(R+\tau)}r(\tau-\lambda)} \cdot \Omega = 0,$$

$$\begin{aligned}\Omega := {} & e^{r(s+2\tau)}r(\lambda-R)^{1+\eta} - e^{r(R+s+T+\tau)}\omega - e^{r(R+T+2\tau)}r(\tau-\lambda)\omega \\ & + e^{r(s+T+2\tau)}\left(\omega + r(R-\lambda)\left((\lambda-R)^{\eta}+\omega\right)\right).\end{aligned}$$

Again we have to proceed numerically. We take all parameters from the first numerical experiment and search for values of θ an ψ that lead to the best fit of the historical time series for schooling. We estimate $\theta = 0.087$ and $\psi = 0.08$. Again we feed in the historical time series for life expectancy and predict schooling and retirement. The results are shown in Figure 6. The model fails to predict the dip in schooling around the Civil War period but gets the trend of schooling almost right. For that, we need a comparatively small concavity of the return to

education. Bils and Klenow estimated $\psi = 0.58$, suggesting much more curvature of the return function. But their estimate is for a cross section of 56 developing and developed countries, which makes the numbers hardly comparable. Our within-country specification is more in line with micro-estimates suggesting that there is little evidence of strongly decreasing returns (Card, 1999). With respect to age of retirement and years in retirement this version of the model preserves the already good fit of the previous numerical experiment.

FIGURE 6: DATA AND MODEL PREDICTION: 1840-1970 (DECREASING RETURNS)



Solid lines: data from Figure 1. Dashed lines: model prediction. Parameters as for Figure 5 and $\theta = 0.087$ and $\psi = 0.08$.

4. CONCLUSION

In this paper we have proposed a theory based on human aging that helps to understand the long-run trends of life expectancy, schooling and retirement. The expectation of more healthy years, or more generally, less early declining labor productivity, induces more schooling. More education and better health increase lifetime income and consumption and induce a higher demand for leisure, i.e. a longer stay in retirement. We have also shown that the calibrated model generates quantitatively reasonable long-run trends of schooling and retirement behavior.

In order to illustrate one particular mechanism we have chosen a simple partial equilibrium model that extends Ben-Porath (1967) and Hazan (2009) by one aspect, human aging understood as declining labor productivity. We have thus neglected other potentially important drivers of schooling and retirement behavior. We have, for example, ignored that individuals may die while still in the workforce, as suggested by Cervelatti and Sunde (2012), that preferences may

be non-homothetic and that individuals demand education for pleasure, as suggested by Restuccia and Vandenbroucke (2013), and that individuals may actively invest in their health to raise productivity and to live longer, as suggested by Dalgaard and Strulik (2012). Furthermore the public economics literature emphasizes fiscal incentives as an important driver of retirement (e.g. Gruber and Wise, 1998) and the growth and human capital literature emphasizes technological change and globalization as important drivers of demand for an educated workforce (e.g. Galor and Weil, 2000; Galor and Mountford, 2008). Combining "our" mechanism with these complementing channels would certainly further improve the understanding of long-run trends of schooling and retirement.

Appendix A. Derivation of the optimal values

The interior solution of the optimization problem of the household is derived from the FOCs (5) and (6), i.e.

$$0 \stackrel{!}{=} \theta + \frac{2(\lambda-\tau)}{R^2 - 2\lambda R + 2s(\lambda-\tau) + \tau^2}, \tag{13}$$

$$0 \stackrel{!}{=} \frac{2T(R-\lambda)}{R^2 - 2R\lambda + 2s(\lambda-\tau) + \tau^2} - (\lambda - R)^{-\eta}\omega. \tag{14}$$

Rearrange equation (13) to obtain

$$\frac{2}{R^2 - 2R\lambda + 2s(\lambda-\tau) + \tau^2} = -\frac{\theta}{\lambda-\tau}$$

and insert this into equation (14) to arrive at

$$\omega(\lambda - R)^{-\eta} = -\frac{T\theta(R-\lambda)}{\lambda-\tau} \quad \Leftrightarrow \quad R = \lambda - \left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}. \tag{15}$$

The optimal amount of schooling follows from inserting the optimal retirement age R from (15) into equation (14), i.e.

$$s = \frac{\lambda+\tau}{2} - \frac{1}{\theta} - \frac{\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{2}{1+\eta}}}{2(\lambda-\tau)}. \tag{16}$$

Therefore, the optimal labor supply is, given by $L = R - s$, is

$$L = \frac{1}{\theta} + \frac{1}{2(\lambda-\tau)}\left(\tau - \lambda + \left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}\right)^2. \tag{17}$$

If the Hessian of U is negative definite in the critical point (s, R), then this point is a local maximum. The Hessian of U is given by

$$H_U(s,R) := \begin{pmatrix} \frac{\partial^2 U}{\partial s^2} & \frac{\partial^2 U}{\partial s \partial R} \\ \frac{\partial^2 U}{\partial R \partial s} & \frac{\partial^2 U}{\partial R^2} \end{pmatrix} =: \begin{pmatrix} H_{1,1} & H_{1,2} \\ H_{2,1} & H_{2,2} \end{pmatrix}, \tag{18}$$

where

$$\begin{aligned}
H_{1,1} &= \frac{2T(-R^2 + 2R\lambda + 2(s-\lambda)\lambda - 2s\tau + \tau^2)}{(R^2 - 2R\lambda + 2s(\lambda-\tau) + \tau^2)^2} - \eta\omega(\lambda - R)^{-1-\eta}, \\
H_{1,2} &= -\frac{4T(R-\lambda)(\lambda-\tau)}{(R^2 - 2R\lambda + 2s(\lambda-\tau) + \tau^2)^2}, \\
H_{2,1} &= H_{1,2}, \\
H_{2,2} &= -\frac{4T(\lambda-\tau)^2}{(R^2 - 2R\lambda + 2s(\lambda-\tau) + \tau^2)^2}.
\end{aligned}$$

The two principal minors of H evaluated in the critical point are

$$H_{U,1} = -\eta\frac{T\theta}{(\lambda-\tau)} - \frac{T\theta\left(\lambda - \tau + \theta\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{2}{1+\eta}}\right)}{(\lambda-\tau)^2} < 0, \tag{19}$$

$$H_{U,2} = \det H(R,s) = \frac{T^2\theta^3}{\lambda-\tau}(1+\eta) > 0. \tag{20}$$

Hence, the Hessian is negative definite and the critical point is a maximum.

Appendix B. Proofs of the Propositions

Proof of Proposition 1. The partial derivatives of s, c.f. (8), with respect to T, τ, θ are

$$\begin{aligned}
\frac{\partial s}{\partial T} &= \frac{\omega\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1-\eta}{1+\eta}}}{T^2(1+\eta)\theta} > 0,\\
\frac{\partial s}{\partial \theta} &= \frac{1}{\theta^2}\left(1 + \frac{\omega\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1-\eta}{1+\eta}}}{T(1+\eta)}\right) > 0,\\
\frac{\partial s}{\partial \tau} &= \frac{1}{2}\left(1 + \frac{(1-\eta)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{2}{1+\eta}}}{(1+\eta)(\lambda-\tau)^2}\right).
\end{aligned}$$

For $\eta \leq 1$ it is easy to see that $\frac{\partial s}{\partial \tau} > 0$. If $\eta > 1$, it holds that

$$1 + \frac{(1-\eta)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{2}{1+\eta}}}{(1+\eta)(\lambda-\tau)^2} > 0 \;\Leftrightarrow\; (1+\eta)(\lambda-\tau)^2 > (\eta-1)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{2}{1+\eta}}$$

This inequality is true because

$$(\eta-1)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{2}{1+\eta}} \leq (\eta-1)(\lambda-\tau)^2 \overset{!}{<} (1+\eta)(\lambda-\tau)^2 \;\Leftrightarrow\; \eta - 1 < 1 + \eta.$$

□

Proof of Proposition 2. The partial derivatives of R, c.f. (9), with respect to T, τ, θ and ω are

$$\begin{aligned}
\frac{\partial R}{\partial T} &= \frac{\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}}{T(1+\eta)} > 0,\\
\frac{\partial R}{\partial \tau} &= \frac{\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}}{(1+\eta)(\lambda-\tau)} > 0,\\
\frac{\partial R}{\partial \theta} &= \frac{\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}}{\theta(1+\eta)} > 0,\\
\frac{\partial R}{\partial \omega} &= -\frac{\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}}{\omega(1+\eta)} < 0.
\end{aligned}$$

□

Proof of Proposition 3. The partial derivatives of L, c.f. (10), with respect to T and τ are

$$\frac{\partial L}{\partial T} = -\frac{\omega\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{-\eta}{1+\eta}}}{T^2(1+\eta)\theta}\left(-\lambda+\tau+\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}\right),$$

$$\frac{\partial L}{\partial \tau} = \frac{\left(-\lambda+\tau+\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}\right)\left((1+\eta)(\lambda-\tau)+(\eta-1)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}\right)}{2(1+\eta)(\lambda-\tau)^2}.$$

We have $\frac{\partial L}{\partial T} > 0$ because

$$\frac{\omega\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{-\eta}{1+\eta}}}{T^2(1+\eta)\theta} \geq 0 \text{ and } \left(-\lambda+\tau+\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}\right) = \tau - R \leq 0.$$

Furthermore,

$$\begin{aligned}\frac{\partial L}{\partial \tau} < 0 \;&\Leftrightarrow\; \left((1+\eta)(\lambda-\tau)+(\eta-1)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}\right) > 0\\ &\Leftrightarrow (1+\eta)(\lambda-\tau)+(\eta-1)\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}} > 0\\ &\Leftrightarrow\; 1 > \frac{1-\eta}{(1+\eta)(\lambda-\tau)}\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}}.\end{aligned}$$

For $\eta \leq 1$ it is obvious that the above inequality holds. Assume now $\eta > 1$, then we have

$$\frac{1-\eta}{(1+\eta)(\lambda-\tau)}\left(\frac{(\lambda-\tau)\omega}{\theta T}\right)^{\frac{1}{1+\eta}} = \frac{1-\eta}{(1+\eta)(\lambda-\tau)}(\lambda-R) \leq \frac{1-\eta}{(1+\eta)} < 1 \;\forall\; \eta > 0.$$

□

Proof of Proposition 4. An equiproportional increase in τ and T can be described by the directional derivative $\frac{\partial L}{\partial T} + \frac{\partial L}{\partial \tau}$, i.e.

$$\frac{\partial L}{\partial T} + \frac{\partial L}{\partial \tau} = \frac{\left(-\lambda+\tau+\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}\right)}{2T^2(1+\eta)\theta(\lambda-\tau)^2}\cdot\Lambda \tag{21}$$

with

$$\Lambda := -\omega\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{-\eta}{1+\eta}} 2(\lambda-\tau)^2 + T^2\theta\left((1+\eta)(\lambda-\tau)+(\eta-1)\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}\right).$$

For the numerator of the first term of equation (21) it holds that

$$\left(-\lambda+\tau+\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}\right) = \tau - R < 0.$$

The denominator is greater than 0. Therefore, the problem simplifies to

$$-\omega\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{-\eta}{1+\eta}} 2(\lambda-\tau)^2 + T^2\theta\left((1+\eta)(\lambda-\tau)+(\eta-1)\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}\right) \overset{!}{>} 0$$

$$\Leftrightarrow \frac{\omega}{T^2\theta}\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{-\eta}{1+\eta}} 2(\lambda-\tau)^2 - (\eta-1)\left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}} < (1+\eta)(\lambda-\tau)$$

$$\Leftrightarrow \left(\frac{(\lambda-\tau)\omega}{T\theta}\right)^{\frac{1}{1+\eta}}\left[\frac{2(\lambda-\tau)^2\omega}{T^2\theta}\frac{T^2\theta}{(\lambda-\tau)\omega} - (\eta-1)\right] < (1+\eta)(\lambda-\tau)$$

$$\Leftrightarrow \left(\frac{(\lambda-\tau)\omega}{T}\right)^{\frac{1}{1+\eta}}\left[\frac{2(\lambda-\tau)+T(1-\eta)}{T(1+\eta)(\lambda-\tau)}\right] < \theta^{\frac{1}{1+\eta}}$$

$$\Leftrightarrow \theta > \frac{(\lambda-\tau)\omega}{T}\left[\frac{2(\lambda-\tau)+T(1-\eta)}{T(1+\eta)(\lambda-\tau)}\right]^{1+\eta}.$$

□

Proof of Proposition 5. The partial derivatives of s, c.f. (10), with respect to T, τ, ω and θ are

$$\begin{aligned}
\frac{\partial s}{\partial \tau} &= \frac{1}{2}\left(1+\frac{\omega^2}{T^2\theta^2}\right) > 0,\\
\frac{\partial s}{\partial T} &= \frac{(\lambda-\tau)\omega^2}{T^3\theta^2} > 0,\\
\frac{\partial s}{\partial \omega} &= \frac{(\tau-\lambda)\omega}{T^2\theta^2} < 0,\\
\frac{\partial s}{\partial \theta} &= \frac{\theta+\frac{(\lambda-\tau)\omega^2}{T^2}}{\theta^3} > 0.
\end{aligned}$$

□

Proof of Proposition 6. The partial derivatives of R, c.f. equation (11), with respect to T, τ, ω and θ are

$$\begin{aligned}
\frac{\partial R}{\partial \tau} &= \frac{\omega}{T\theta} > 0,\\
\frac{\partial R}{\partial T} &= \frac{(\lambda-\tau)\omega}{T^2\theta} > 0.\\
\frac{\partial R}{\partial \omega} &= \frac{\tau-\lambda}{T\theta} < 0.\\
\frac{\partial R}{\partial \theta} &= \frac{(\lambda-\tau)\omega}{T\theta^2} > 0.
\end{aligned}$$

□

Proof of Proposition 7. The partial derivatives of L, c.f. equation (12), with respect to T, τ, and ω are

$$\begin{aligned}
\frac{\partial L}{\partial \tau} &= -\frac{(\omega-T\theta)^2}{2T^2\theta^2} < 0\\
\frac{\partial L}{\partial T} &= \frac{(\lambda-\tau)(T\theta-\omega)\omega}{T^3\theta^2} < 0 \;\Leftrightarrow\; \omega > T\theta \Leftrightarrow \theta < \frac{\omega}{T}\\
\frac{\partial L}{\partial \omega} &= \frac{(\lambda-\tau)(\omega-T\theta)}{T^2\theta^2} < 0 \;\Leftrightarrow\; \omega < T\theta \Leftrightarrow \theta > \frac{\omega}{T}
\end{aligned}$$

□

Proof of Proposition 8. An equiproportional increase in τ and T can be described by the directional derivative $\frac{\partial L}{\partial T} + \frac{\partial L}{\partial \tau}$. In the special case with $\eta = 0$ this provides

$$\frac{\partial L}{\partial T} + \frac{\partial L}{\partial \tau} = -\frac{(T\theta - \omega)(T^2\theta - \omega(T + 2(\lambda - \tau)))}{2T^3\theta^2} \overset{!}{<} 0$$
$$\Leftrightarrow \ \theta < \frac{\omega}{T} \text{ or } \theta > \frac{\omega(T + \lambda - \tau)}{T^2}.$$

□

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